# TRIPLETS and TRIANGLES 

Hosted by Logic Masters India<br>February 2016<br>\section*{Puzzles set by David McNeill}<br>Tested by Tom Collyer, Yuhei Kusui and Robert Vollmert

This Sudoku set is brought to you by the number 3. Puzzles 1-3 are classics. Puzzles 4-6 and 10 are standard variations. Puzzles 7-9 are slightly modified variations. Puzzles 11-14 are more novel. The instruction booklet explains the rules of each type accompanied by an example.

## Details

- The test will last for 90 minutes
- The competition booklet will have 14 pages, each with a single puzzle
- Each puzzle has a marked row and marked column for solution entry
- When submitting solutions, enter only the digits in the row/column in order, ignoring the black triangles in puzzles 13 and 14
- Instant grading will be used
- On-line solving is not available
- The puzzle points are shown in the table below
- Solvers who complete all puzzles correctly within the time can claim 10 bonus points for every full minute saved

| Points Table |  |  |
| :---: | :--- | :---: |
| Puzzle |  | Points |
| 1 | Classic | 15 |
| 2 | Classic | 20 |
| 3 | Classic | 30 |
| 4 | Trio | 15 |
| 5 | Anti-Diagonal | 30 |
| 6 | Outside Sums | 70 |
| 7 | Max/Min Triplet Sums | 80 |
| 8 | Thropki | 100 |
| 9 | Thropki | 80 |
| 10 | Tight Fit | 35 |
| 11 | Non-Consecutive Squeeze | 25 |
| 12 | Renban Squeeze | 30 |
| 13 | Triangular Sums | 75 |
| 14 | Arrowhead | 45 |
| Total Points |  | 650 |

We hope you enjoy the puzzles. Good luck.

## Classic

Complete the grid so that each row, column and $3 x 3$ box contains the digits 1-9.

|  | 4 |  | 1 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 5 |  | 8 |  |  | 6 | 3 | 4 |
|  | 7 | 3 | 4 |  | 5 | 8 |  |  |
|  |  | 5 |  |  |  | 4 | 6 | 9 |
| 1 | 8 | 4 |  |  |  | 5 |  |  |
|  |  | 8 | 3 |  | 7 | 2 | 5 |  |
| 6 | 1 | 2 |  |  | 8 |  | 4 |  |

## Trio

Complete the grid so that each row, column and $3 x 3$ box contains the digits 1-9. In addition, each cell marked with a circle must contain one of the digits 1-3, each cell marked with a square must contain one of the digits 4-6, and each of the remaining cells must contain one of the digits 7-9.


## Anti-Diagonal

Complete the grid so that each row, column and $3 \times 3$ box contains the digits 1-9. In addition, each marked diagonal must contain only three different digits.

|  | 7 |  |  |  | 5 |  | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 |  | 5 |  | 3 |  |  |  |
|  |  |  | 4 |  |  |  | 3 |
| 7 |  |  |  |  |  | 1 |  |
|  | 8 |  |  |  |  |  | 4 |
|  |  | 4 |  |  |  |  |  |
|  | 3 |  |  | 2 | 2 |  |  |
| 9 |  |  |  | 7 |  | 3 |  |
|  | 4 |  | 3 |  |  |  | 5 |

## Outside Sums

Complete the grid so that each row, column and $3 \times 3$ box contains the digits 1-9. Each clue outside the grid is the sum of the first three digits in the corresponding row or column.


## Max/Min Triplet Sums

Complete the grid so that each row, column and $3 \times 3$ box contains the digits 1-9. Each clue outside the grid is either the maximum or minimum sum of three consecutive digits observed in the corresponding row or column.


## Thropki

Complete the grid so that each row, column and $3 \times 3$ box contains the digits 1-9. Neighbouring cells containing digits with a difference of 3 are marked with a white triangle. Neighbouring cells containing digits with a quotient of 3 are marked with a black triangle. All possible triangles are given.


## Tight Fit

Complete the grid so that each row, column and $2 \times 3$ box contains the digits 1-9. In addition, within each square which is subdivided into two triangles, the smaller digit must lie above the larger digit.


## Non-Consecutive Squeeze

Complete the grid so that each row, column and $2 \times 3$ box contains the digits 1-9. In addition, cells sharing an edge must not contain consecutive digits. The Tight Fit constraint about smaller digits having to lie above larger digits in split squares does not apply.


## Renban Squeeze

Complete the grid so that each row, column and $2 \times 3$ box contains the digits 1-9. In addition, each shaded region must contain a set of consecutive digits. The Tight Fit constraint about smaller digits having to lie above larger digits in split squares does not apply.


## Triangular Sums

Complete the grid so that each row, column and $3 \times 3$ box contains the digits 1-9. In addition, within a square which is split diagonally, one of the triangles must be coloured black. Two black triangles may not share an edge, nor may a black triangle share an edge with the grid boundary. The three digits in the cells surrounding each of the black triangles must add up to a triangular number. The only triangular numbers possible are $6,10,15$ and 21 .


## Arrowhead

Complete the grid so that each row, column and $3 x 3$ box contains the digits 1-9. In addition, within a square which is split diagonally, one of the triangles must be coloured black. This triangle acts as a symmetrical arrowhead. The digit placed in the other triangle must equal the sum of the first two digits pointed at by the corresponding arrowhead.

|  |  | 3 |  |  |  | 5 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 5 |  | 4 |  | 8 |  |  |  |
| 1 |  |  |  | 3 |  |  |  |  |
|  |  |  | 5 |  |  |  | 3 |  |
|  |  | 7 |  | 1 |  | 9 |  |  |
|  | 3 |  |  |  | 2 |  |  |  |
|  |  |  |  | 7 |  |  |  | 1 |
|  |  |  | 1 |  | 3 |  | 9 |  |


| 8 | 4 | 6 | 1 | 3 | 2 | 7 | 9 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 5 | 1 | 8 | 7 | 9 | 6 | 3 | 4 |
| 9 | 7 | 3 | 4 | 6 | 5 | 8 | 1 | 2 |
| 3 | 2 | 5 | 7 | 8 | 1 | 4 | 6 | 9 |
| 7 | 6 | 9 | 5 | 4 | 3 | 1 | 2 | 8 |
| 1 | 8 | 4 | 2 | 9 | 6 | 5 | 7 | 3 |
| 4 | 9 | 8 | 3 | 1 | 7 | 2 | 5 | 6 |
| 6 | 1 | 2 | 9 | 5 | 8 | 3 | 4 | 7 |
| 5 | 3 | 7 | 6 | 2 | 4 | 9 | 8 | 1 |


| 8 | 7 | 3 | 2 | 1 | 5 | 4 | 9 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 | 2 | 5 | 6 | 3 | 9 | 8 | 1 | 7 |
| 6 | 1 | 9 | 4 | 8 | 7 | 2 | 3 | 5 |
| 7 | 5 | 2 | 9 | 4 | 6 | 1 | 8 | 3 |
| 1 | 8 | 6 | 7 | 2 | 3 | 5 | 4 | 9 |
| 3 | 9 | 4 | 1 | 5 | 8 | 7 | 6 | 2 |
| 5 | 3 | 1 | 8 | 6 | 2 | 9 | 7 | 4 |
| 9 | 6 | 8 | 5 | 7 | 4 | 3 | 2 | 1 |
| 2 | 4 | 7 | 3 | 9 | 1 | 6 | 5 | 8 |



| 5 | $7 / 9$ | 4 | $1 / 2$ | 6 | $3 / 8$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1 / 8$ | 6 | $2 / 3$ | 9 | $4 / 5$ | 7 |
| 7 | $3 / 4$ | 1 | 5 | 8 | 9 |
| $2 / 6$ |  |  |  |  |  |
| $2 / 6$ | 8 | $5 / 9$ | 7 | $1 / 3$ | 4 |
| 3 | $1 / 2$ | 7 | $4 / 6$ | 8 | $5 / 9$ |
| $4 / 9$ | 5 | $6 / 8$ | 3 | $2 / 7$ | 1 |


| $2 / 8$ | 3 | 1 | 5 | 7 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | $9 / 4$ | 7 | 3 | 8 | 1 |
| $1 / 2$ |  |  |  |  |  |
| 7 | 2 | 5 | 3 | $8 / 4$ | 6 |
| 4 | 8 |  |  |  |  |
| 4 | 8 | 6 | $1 / 7$ | 2 | $5 / 3$ |
| 6 | 1 | 1 | 4 | 2 | $5 / 3$ |
| 3 | 5 | 8 | 2 | 8 | 8 |


|  | $4^{7}$ | 5 | 6 | $2^{9}$ | 93 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 63 | 2 | 9 | $7{ }^{4}$ | 1 | $5^{8}$ |
| 2 | 9 | 16 | 85 | $4^{3}$ | 3 |
| 4 | 53 | 8 | $9 / 1$ | 6 | 2 |
| 97 | 8 | $2^{4}$ | 3 | 5 | $6^{1}$ |
| 5 | $1{ }^{6}$ | 3 | 2 | 8 | 749 |


| 6 | 5 | 7 | 3 | 4 | 9 | 8 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 | 8 | 2 | 6 | 1 | 7 | 3 | 9 | 5 |
| 9 | 1 | 3 | 8 | 2 | 5 |  | 7 | 4 |
| 7 | 9 | 1 | 4 | 5 | 3 | 2 | 6 | 8 |
| 5 | 6 | 4 | 2 | 8 | 1 | 9 | 7 | 3 |
| 3 | 2 | 8 | 9 | 7 | 6 | 4 | 5 | 1 |
| 2 | 4 | 9 | 5 | 6 | 8 | 1 |  | 3 |
| 8 | 7 | 5 | 1 | 3 | 4 | 6 | 2 | 9 |
| 1 | 3 | 6 | 7 | 9 | 2 | 5 | 8 | 4 |


| 4 | 8 | 3 | 6 | 2 | 1 | 5 | 7 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 7 | 5 | 2 | 4 | 9 | 8 | 1 | 6 | 3 |
| 1 | 9 | 6 | 7 | 3 | 5 | 8 | 4 | 2 |
| 9 | 2 | 1 | 5 | 6 | 7 | 4 | 3 | 8 |
| 8 | 6 | 7 | 3 | 1 | 4 | 9 | 2 | 5 |
| 5 | 3 | 4 | 9 | 2 | 2 | 7 | 1 | 6 |
| 6 | 4 | 5 | 2 | 7 | 9 | 3 | 8 | 1 |
| 2 | 7 | 8 | 1 | 5 | 3 | 6 | 9 | 4 |
| 3 | 1 | 9 | 8 | 4 | 6 | 2 | 5 | 7 |

